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- Lecture 1 (7 March, 9:15-10:45) :  
Qubits, entanglement and Bell's inequalities.
- Lecture 2 (14 March, 11:00-12:30) :  
From QND measurements to quantum gates and quantum information.
- Lecture 3 (21 March, 9:15-10:45) :  
Quantum cryptography with discrete and continuous variables.
- Lecture 4 (28 March, 11:10-12:30) :  
Non-Gaussian quantum optics and optical quantum networks.

**Part 1 - Quantum optics with discrete and continuous variables**

- 1.1 Homodyne detection and quantum tomography
- 1.2 Generating non-Gaussian Wigner functions : kittens, cats and beyond

**Part 2 - Towards optical quantum networks**

- 2.1 Entanglement, teleportation, and quantum repeaters
- 2.2 Some experimental achievements

**Part 3 - A close look to a nice single photon**

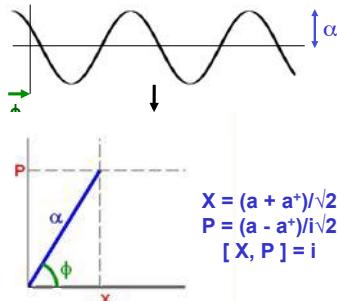
- 3.1 Single photons: from old times to recent ones
- 3.2 Experimental perspectives

**Quantum description of light**

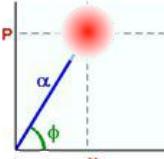


A single "mode" of the quantized electromagnetic field (a plane wave, or a "Fourier transform limited" pulse) is described as a quantized harmonic oscillator : operators  $a, a^+$ ,  $N = a^+ a$ , etc...

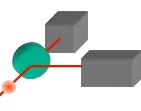
**Quantum description of light**

Parameters :	Discrete  Photons Number of photons $n$ Destruction operators $a$ Creation operators $a^+$ Number operator $N = a^+ a$	Continuous  Wave Amplitude & Phase (polar) Quadratures $X$ & $P$ (cartesian)
		 $X = (a + a^+)/\sqrt{2}$ $P = (a - a^+)/i\sqrt{2}$ $[X, P] = i$

## Quantum description of light

	Discrete Photons	Continuous Wave
Parameters :	Number & Coherence	Amplitude & Phase (polar) Quadratures X & P (cartesian)
Representation:	Density matrix $\rho = \begin{bmatrix} \rho_{0,0} & \rho_{0,1} & \rho_{0,2} & \dots \\ \rho_{1,0} & \rho_{1,1} & \rho_{1,2} & \dots \\ \rho_{2,0} & \rho_{2,1} & \rho_{2,2} & \dots \\ \dots & \dots & \dots & \dots \end{bmatrix}$ Coherences $\langle n   \rho   m \rangle$	Wigner function $W(X,P)$  $X = (a + a^\dagger)/\sqrt{2}$ $P = (a - a^\dagger)/i\sqrt{2}$ $[X, P] = i$  Heisenberg : $\Delta X \cdot \Delta P \geq 1/2$ <del>measurement of both X and P</del> <del>measurement of <math>X_\theta = X \cos\theta + P \sin\theta</math></del>

## Quantum description of light

	Discrete Photons	Continuous Wave
Parameters :	Number & Coherence	Amplitude & Phase (polar) Quadratures X & P (cartesian)
Representation:	Density matrix	Wigner function $W(X,P)$
Measurement:	Counting : APD, VLPC, TES...	Demodulation : Homodyne detection  Local Oscillator Quantum state $\theta$ $V_1 - V_2 \propto E_{OL}E_{EQ}(\theta)$ $\propto X_\theta = X \cos\theta + P \sin\theta$ Interference, then subtraction of photocurrents :

### Homodyne detection

$$I_1 = |E_{LO} + E_S|^2 / 2 = \{ |E_{LO}|^2 + |E_S|^2 + |E_{LO}| (E_S e^{-i\theta_{LO}} + E_S^* e^{i\theta_{LO}}) \} / 2$$

$$I_2 = |E_{LO} - E_S|^2 / 2 = \{ |E_{LO}|^2 + |E_S|^2 - |E_{LO}| (E_S e^{-i\theta_{LO}} + E_S^* e^{i\theta_{LO}}) \} / 2$$

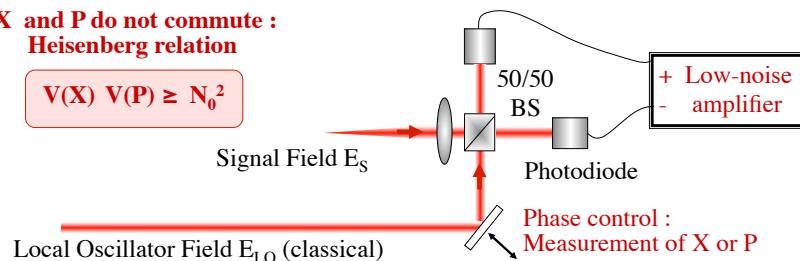
$$I_1 - I_2 = |E_{LO}| (E_S e^{-i\theta_{LO}} + E_S^* e^{i\theta_{LO}})$$

$$= |E_{LO}| (E_S + E_S^*) \Rightarrow \sqrt{n_{LO}} (a + a^\dagger) \quad \text{X meas. } (\theta_{LO} = 0)$$

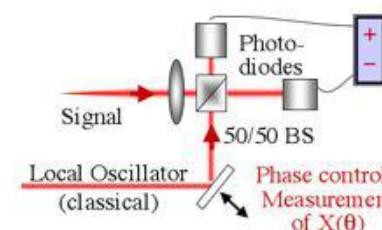
$$= |E_{LO}| (E_S - E_S^*)/i \Rightarrow \sqrt{n_{LO}} (a - a^\dagger)/i \quad \text{P meas. } (\theta_{LO} = \pi/2)$$

**X and P do not commute :**  
Heisenberg relation

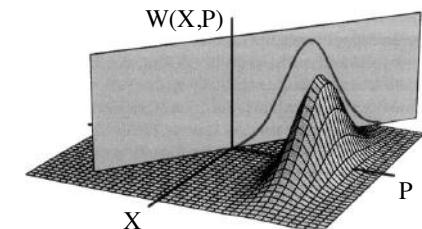
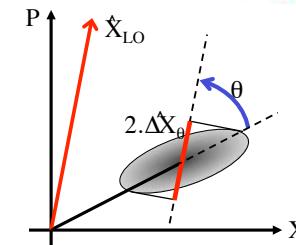
$$V(X) V(P) \geq N_0^2$$



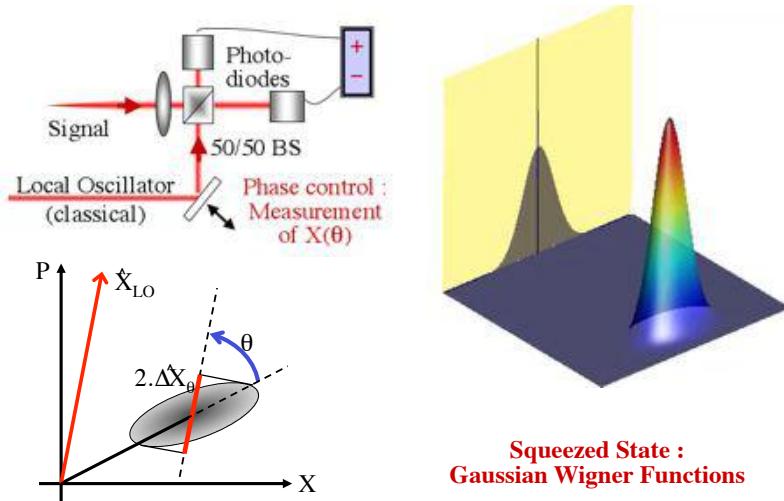
### Homodyne detection, Wigner Function and Quantum Tomography



- Quasiprobability density : Wigner function  $W(X,P)$
- Marginals of  $W(X, P)$   
=> Probability distributions  $P(X)$
- Probability distributions  $P(X\theta)$   
=>  $W(X, P)$  (quantum tomography)



## Homodyne detection, Wigner Function and Quantum Tomography



## Quantum description of light

	Discrete Photons	Continuous Wave
Parameters :	Number & Coherence	Amplitude & Phase (polar) Quadratures X & P (cartesian)
Representation:	Density matrix	Wigner function $W(X,P)$
Measurement :	Counting : APD, VLPC, TES...	Demodulation : Homodyne detection
« Simple » states	Fock states (number states)	Gaussian states
	Sources : - Single atoms or molecules - NV centers in diamond - Quantum dots - Parametric fluorescence ....	Sources : Lasers : coherent states Non-linear media : squeezed states
	$\Delta X \cdot \Delta P \geq 1/2$	$\Delta X \cdot \Delta P \geq 1/2$

## Non-Gaussian States

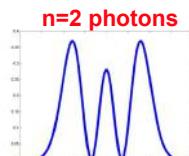
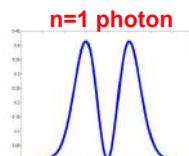
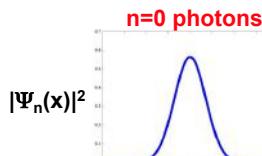
### Basic question :

Consider a single photon : can we speak about its amplitude & phase? quadratures X & P ?

Single mode light field  
Photons  
 $n$  photon state  
Probability  $P_n(X)$



Harmonic oscillator  
Quanta of excitation  
 $n^{\text{th}}$  eigenstate  
Probability  $|\Psi_n(x)|^2$

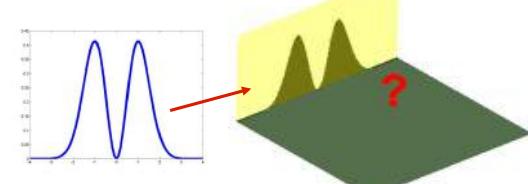


## Non-Gaussian States

### Basic question :

Consider a single photon : can we measure its amplitude & phase? quadratures X & P ?

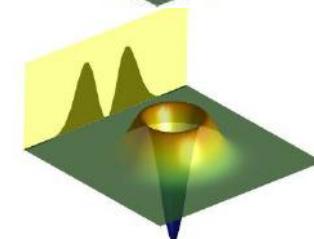
Can the Wigner function of a Fock state  $n = 1$  (with all projections have zero value at origin) be positive everywhere ?



**NO !** The Wigner function must be negative  
It is not a classical statistical distribution !

Hudson-Piquet theorem : for a pure state  $W$  is non-positive iff it is non-gaussian

Many interesting properties for quantum information processing



Wigner function of a single photon state ? (Fock state  $n = 1$ )

$$W(p, q) = \frac{1}{2\pi 2N_0} \int dx e^{\frac{ixp}{2N_0}} \langle q - \frac{x}{2} | \hat{\rho} | q + \frac{x}{2} \rangle$$

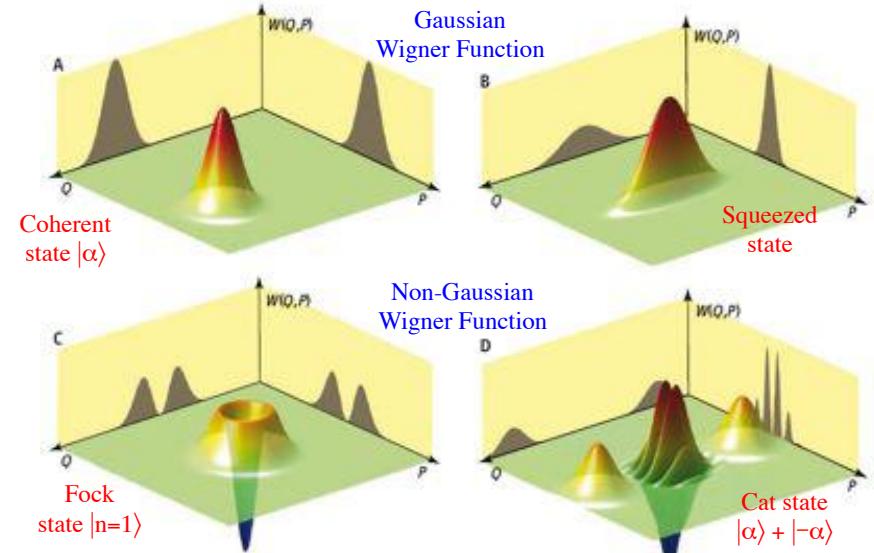
where  $\hat{\rho} = |1\rangle\langle 1|$  and  $N_0$  is the variance of the vacuum noise :

$$[\hat{Q}, \hat{P}] \equiv 2iN_0 \quad \Delta P \Delta Q \geq N_0 \quad N_0 = \Delta P^2 = \Delta Q^2.$$

One may have  $N_0 = \hbar/2$ ,  $N_0 = 1/2$  (theorists),  $N_0 = 1$  (experimentalists)

Using the wave function of the  $n = 1$  state :  $\langle q | 1 \rangle = \frac{q}{(2\pi)^{\frac{1}{4}} N_0^{\frac{3}{4}}} e^{-\frac{q^2}{4N_0}}$

one gets finally :  $W_{|1\rangle}(q, p) = -\frac{1}{2\pi N_0} e^{-\frac{q^2}{2N_0}} \left( 1 - \frac{r^2}{N_0} \right) \quad r^2 = q^2 + p^2$



P. Grangier, "Make It Quantum and Continuous", Science (Perspective) 332, 313 (2011)

## Make It Quantum and Continuous

Philippe Grangier PERSPECTIVES SCIENCE VOL 332 15 APRIL 2011

### Unconditional Quantum Teleportation

A. Furusawa, J. L. Sørensen, S. L. Braunstein, C. A. Fuchs, H. J. Kimble,\* E. S. Polzik  
23 OCTOBER 1998 VOL 282 SCIENCE

### Quantum key distribution using gaussian-modulated coherent states

NATURE | VOL 421 | 16 JANUARY 2003

Frédéric Grosshans\*, Gilles Van Assche†, Jérôme Wenger\*, Rosa Brouri\*, Nicolas J. Cerf† & Philippe Grangier\*

NATURE | VOL 432 | 25 NOVEMBER 2004 | www.nature.com/nature

### Experimental demonstration of quantum memory for light

Brian Julsgaard<sup>1</sup>, Jacob Sherson<sup>1,2</sup>, J. Ignacio Cirac<sup>3</sup>, Jaromír Fiurášek<sup>4</sup> & Eugene S. Polzik<sup>1</sup>

Vol 443 | 5 October 2006 | doi:10.1038/nature05136

### Quantum teleportation between light and matter

Jacob F. Sherson<sup>1</sup>, Hanna Krauter<sup>1</sup>, Rasmus K. Olsson<sup>1</sup>, Brian Julsgaard<sup>1</sup>, Clemens Hammerer<sup>1</sup>, Ignacio Cirac<sup>3</sup> & Eugene S. Polzik<sup>1</sup>

PHYSICAL REVIEW A 68, 042319 (2003)

Quantum computation with optical coherent states  
T. C. Ralph,\* A. Gilchrist, and G. J. Milburn  
W. J. Munro S. Glancy

### Generating Optical Schrödinger Kittens for Quantum Information Processing

Alexei Ourjoumtsev, Rosa Tualle-Brouri,Julien Laurat,Philippe Grangier\*  
SCIENCE VOL 312 7 APRIL 2006

Vol 448 | 16 August 2007 | doi:10.1038/nature06054  
Generation of optical 'Schrödinger cats' from photon number states  
Alexei Ourjoumtsev<sup>1</sup>, Hyunseok Jeong<sup>2</sup>, Rosa Tualle-Brouri<sup>3</sup> & Philippe Grangier<sup>1</sup>

### Teleportation of Nonclassical Wave Packets of Light

Noriyuki Lee,<sup>1</sup> Hugo Bonicht,<sup>2</sup> Yuishi Takeo,<sup>1</sup> Shuntaro Takeda,<sup>3</sup> James Webb,<sup>2</sup>  
Florian Huhnlein<sup>1</sup>, Akira Furusawa<sup>1,4</sup>

15 APRIL 2011 VOL 332 SCIENCE

Small sample, many more papers !



## Content of the Lecture



### Part 1 - Quantum optics with discrete and continuous variables

- 1.1 Homodyne detection and quantum tomography
- 1.2 Generating non-Gaussian Wigner functions : kittens, cats and beyond

### Part 2 - Towards optical quantum networks

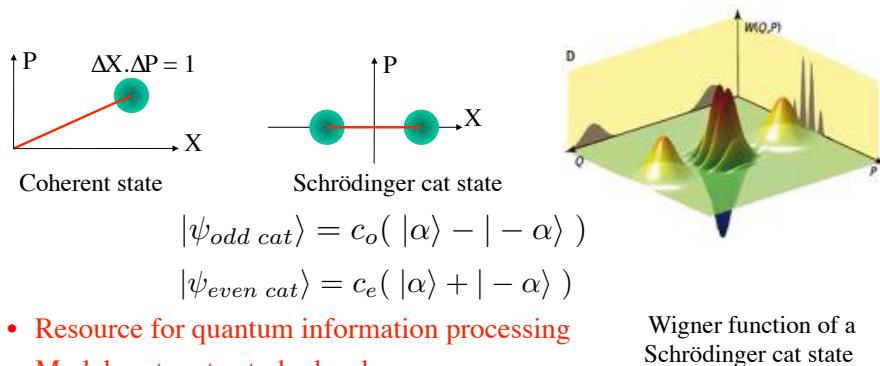
- 2.1 Entanglement, teleportation, and quantum repeaters
- 2.2 Some experimental achievements

### Part 3 - A close look to a nice single photon

- 3.1 Single photons: from old times to recent ones
- 3.2 Experimental perspectives

## « Schrödinger's Cat » state

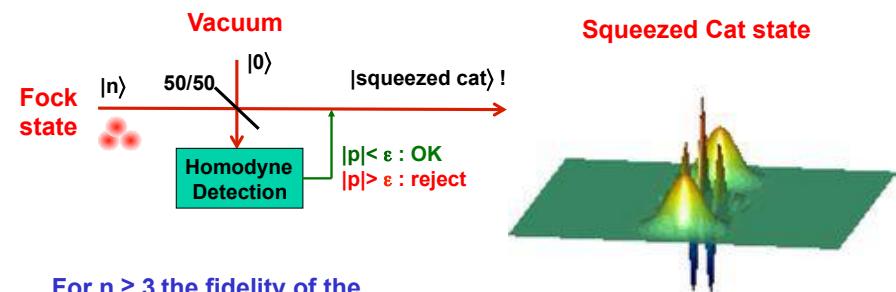
- Classical object in a quantum superposition of distinguishable states
- “Quasi - classical” state in quantum optics : coherent state  $|\alpha\rangle$



- Resource for quantum information processing
- Model system to study decoherence

## How to create a Schrödinger's cat ?

Suggestion by Hyunseok Jeong, proofs by Alexei Ourjoumtsev :

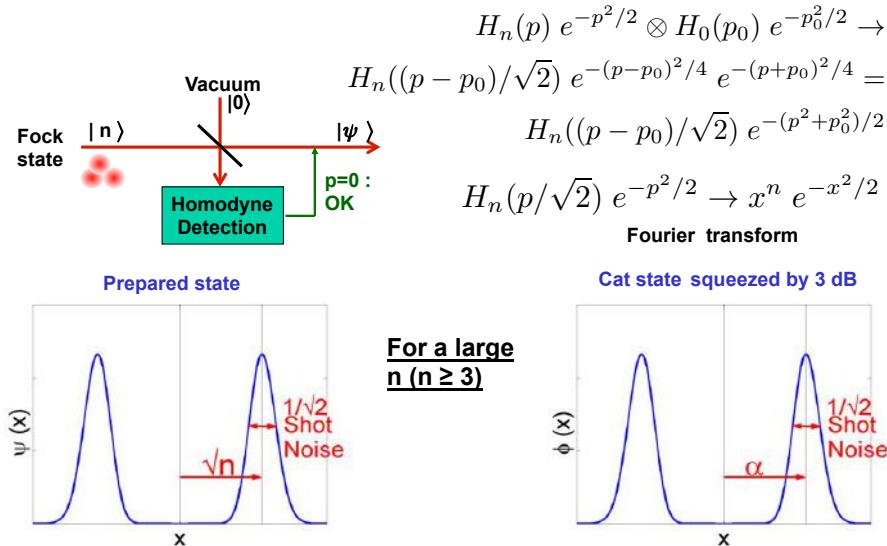


For  $n \geq 3$  the fidelity of the conditional state with a Squeezed Cat state is  $F \geq 99\%$

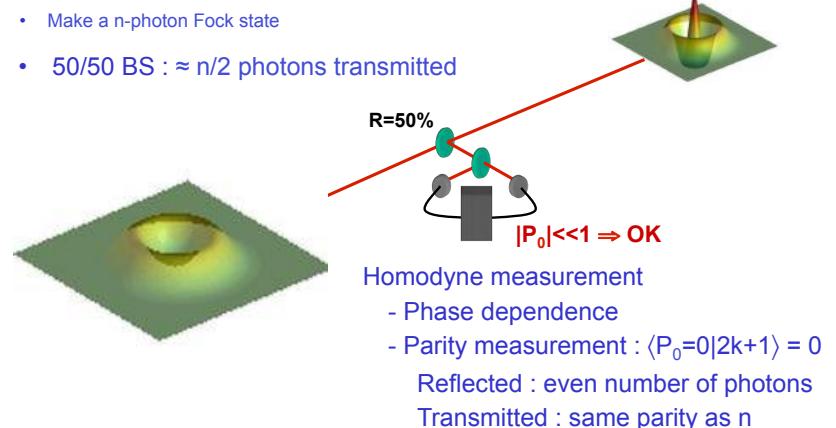
$$S(r)(|\alpha\rangle + e^{i\theta}|-\alpha\rangle)$$

Size :  $\alpha^2 = n$   
Same Parity as  $n$  :  $\theta = n^*\pi$   
Squeezed by : 3 dB

## Another hint...

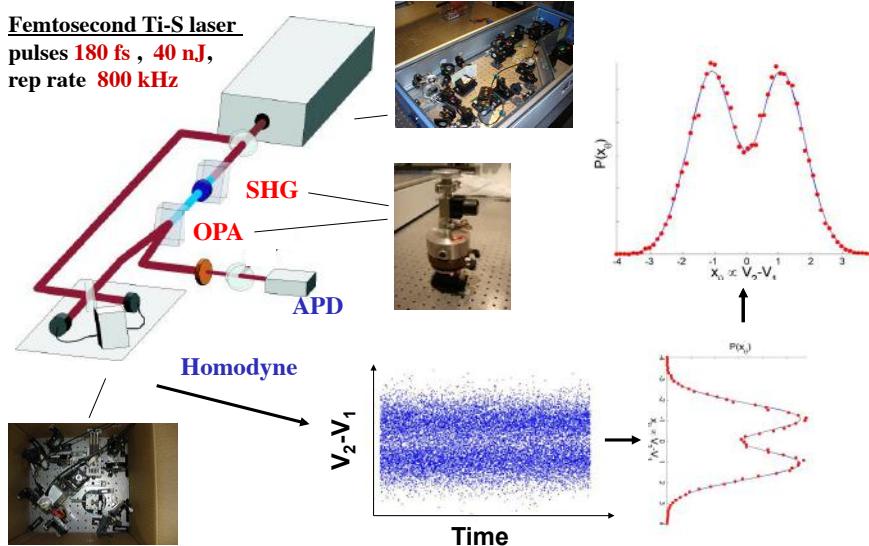


## The rebirth of the cat

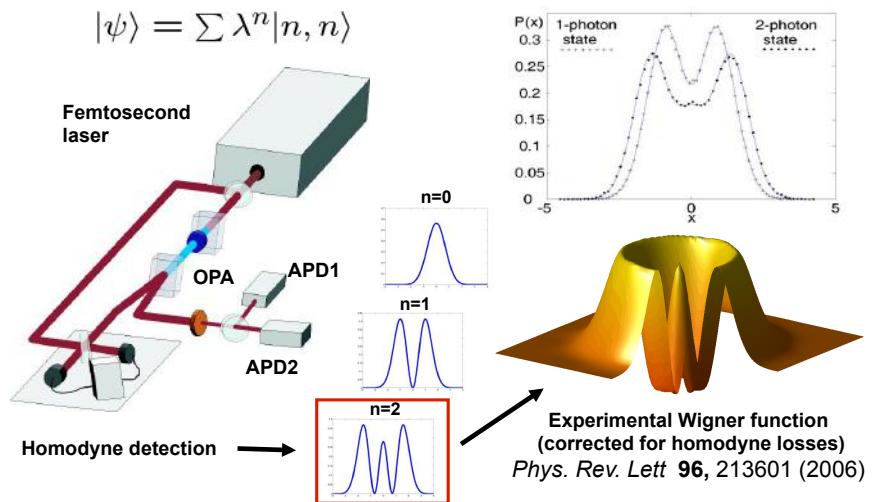


$$\text{Squeezed cat state (from } n=2) = \sqrt{2/3} |2\rangle - \sqrt{1/3} |0\rangle$$

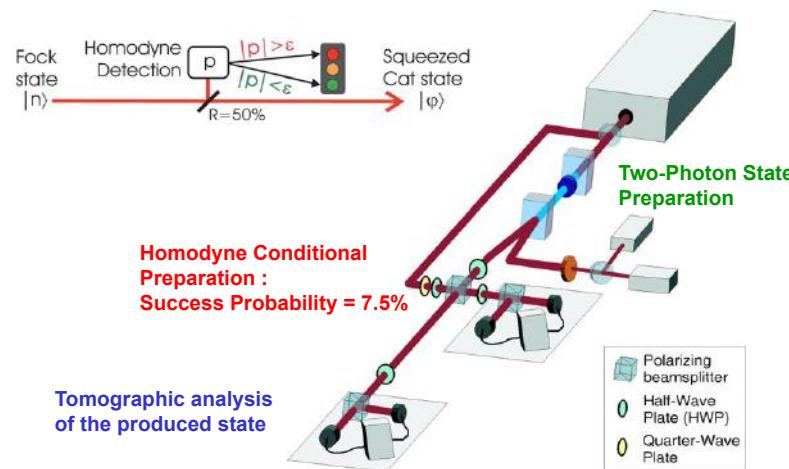
## Experimental Set-up



## Resource : Two-Photon Fock States

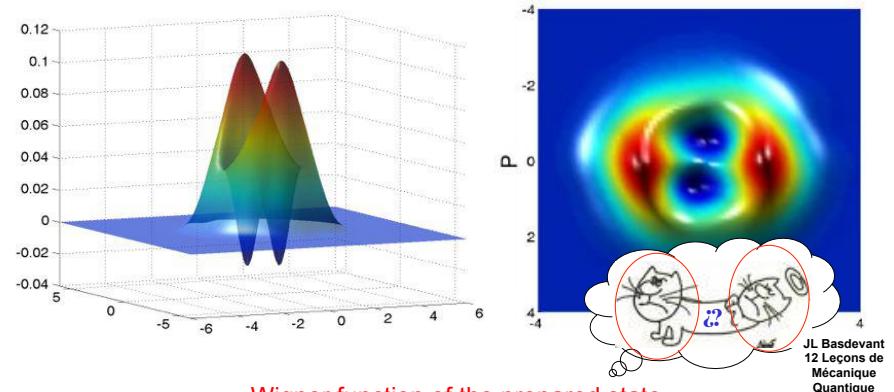


## Squeezed Cat State Generation



## Experimental Wigner function

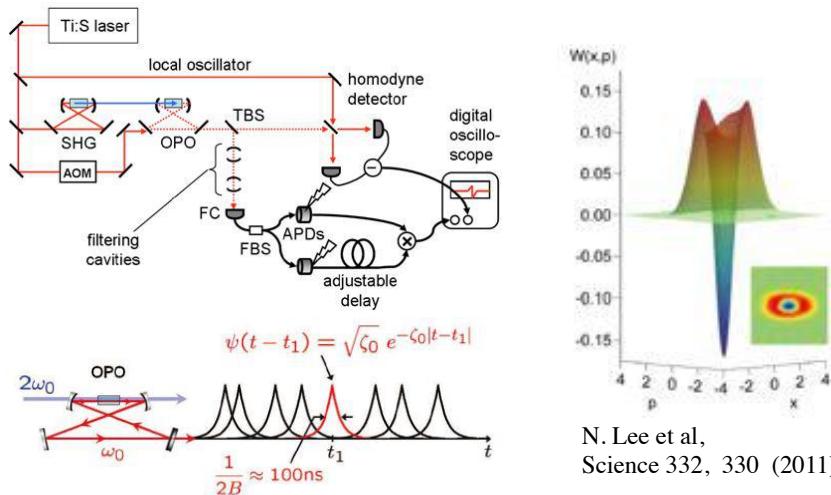
A. Ourjoumtsev et al, Nature **448**, 784, 16 august 2007



Bigger cats : NIST (Gerrits, 3-photon subtraction), ENS (Haroche, microwave cavity QED), UCSB...

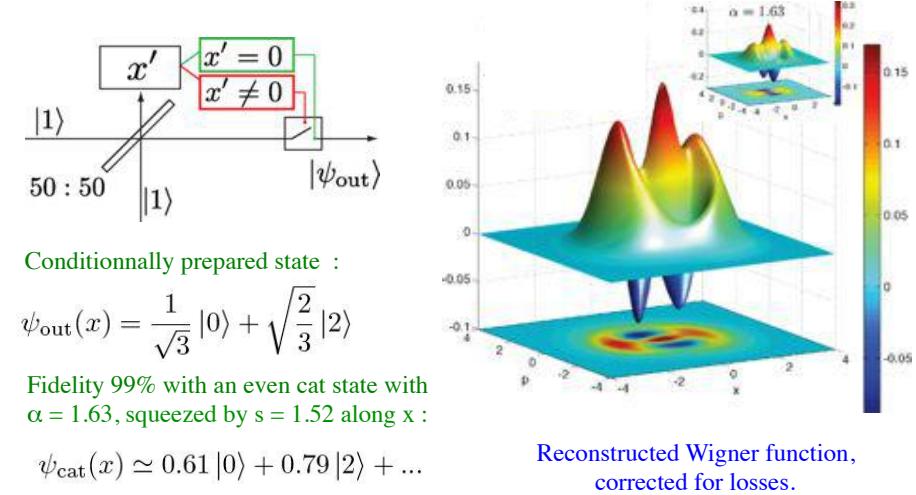
## Schrödinger cats with continuous light beams

Groups of A. Furusawa (Tokyo), M. Sasaki (Tokyo), E. Polzik (Copenhagen), U. Andersen (Copenhagen), J. Laurat (Paris), ....



## Other methods for bigger / better cats...

J. Etesse, M. Bouillard, B. Kanseri, and R. Tualle-Brouri, Phys. Rev. Lett. 114, 193602 (2015)



## Schrödinger cats with microwaves in superconducting cavities

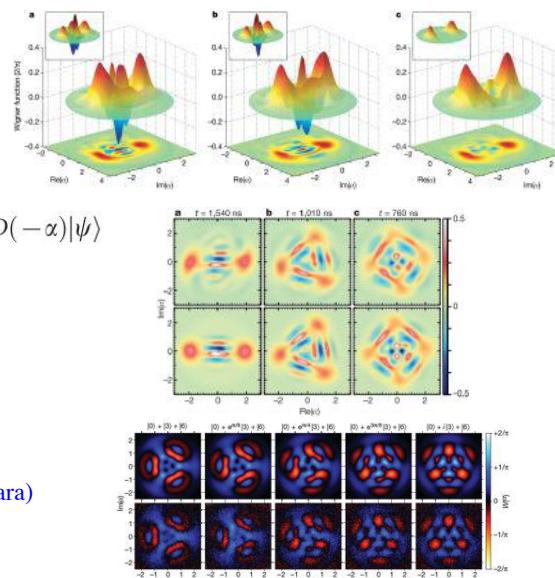
Some examples...

Serge Haroche group  
(cavity QED, Paris)  
Nature 455, 510 (2008)

$$W(\alpha) = \frac{2}{\pi} \langle \psi | D^\dagger(-\alpha) \Pi D(-\alpha) | \psi \rangle$$

Rob Schoelkopf group  
(circuit QED, Yale)  
Nature 495, 205 (2013)  
Cats with 2, 3 or 4 "legs"...

John Martinis group  
(circuit QED, Santa Barbara)  
Nature 459, 546 (2009)  
Quantum state synthesizer



### Part 1 - Quantum optics with discrete and continuous variables

- 1.1 Homodyne detection and quantum tomography
- 1.2 Generating non-Gaussian Wigner functions : kittens, cats and beyond

### Part 2 - Towards optical quantum networks

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## Long distance quantum communications

### How to fight against line losses ?

~~Amplification~~



## Long distance quantum communications

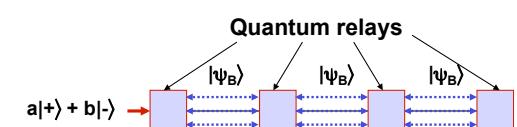
### How to fight against line losses ?

~~Amplification~~



1. Exchange of entangled states

$|\Psi_B\rangle$



Quantum relays

## Long distance quantum communications

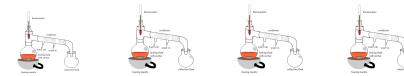
### How to fight against line losses ?

~~Amplification~~



1. Exchange of entangled states

$|\Psi_B\rangle$



2. Entanglement distillation



## Long distance quantum communications

### How to fight against line losses ?

~~Amplification~~



1. Exchange of entangled states

$|\Psi_B\rangle$

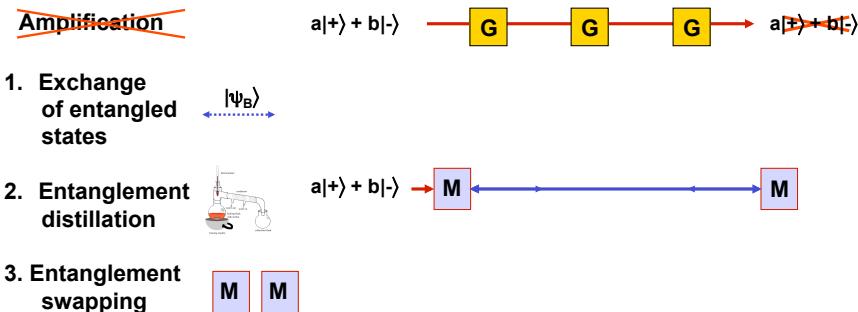


2. Entanglement distillation



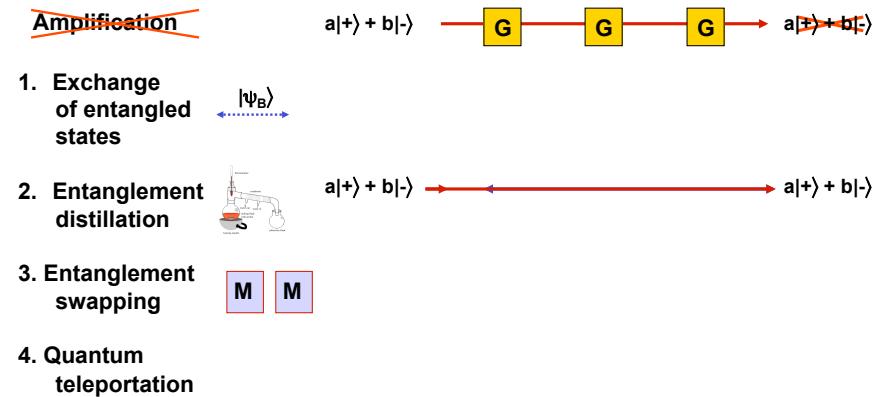
## Long distance quantum communications

### How to fight against line losses ?



## Long distance quantum communications

### How to fight against line losses ?



One needs to :

- \* distribute (many) entangled states
- \* store them (quantum memories)
- \* process them (distillation)



## Quantum Teleportation

C. H. Bennett et al, 1993



1

Qubit in an unknown state  $\Psi$

- \* one cannot « read » it
- \* one cannot duplicate it  
(``non-cloning» theorem)
- \* but it is possible to « teleport » it ?  
(= to make a remote copy,  
destroying the original)

The answer is yes !



## Quantum Teleportation

C. H. Bennett et al, 1993



Step 1

state  $\Psi$

1

Pair of entangled qubits

2  
3

Step 2

Joint Bell measurement

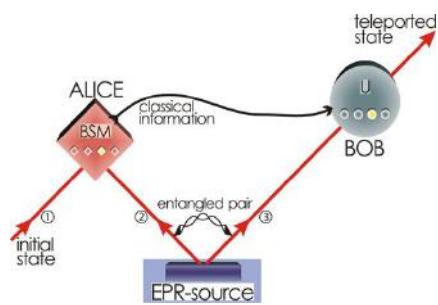
Step 3

result

Operation on qubit 3  
(4 possible operations)

Qubit 3 is now in state  $\Psi$

## Quantum Teleportation



**Initial state**

$$|\Phi\rangle_1 = \alpha|0\rangle_1 + \beta|1\rangle_1$$

**The shared entangled pair**

$$|\Phi^+\rangle_{23} = \frac{1}{\sqrt{2}}(|0\rangle_2|0\rangle_3 + |1\rangle_2|1\rangle_3)$$

$$\begin{aligned} |\Psi\rangle_{123} &= |\Phi\rangle_1 \otimes |\Phi^+\rangle_{23} \\ &= |\Phi^+\rangle_{12} \otimes (\alpha|0\rangle_3 + \beta|1\rangle_3) + \\ &\quad |\Phi^-\rangle_{12} \otimes (\alpha|0\rangle_3 - \beta|1\rangle_3) + \\ &\quad |\Psi^+\rangle_{12} \otimes (\alpha|1\rangle_3 + \beta|0\rangle_3) + \\ &\quad |\Psi^-\rangle_{12} \otimes (\alpha|1\rangle_3 - \beta|0\rangle_3), \end{aligned}$$

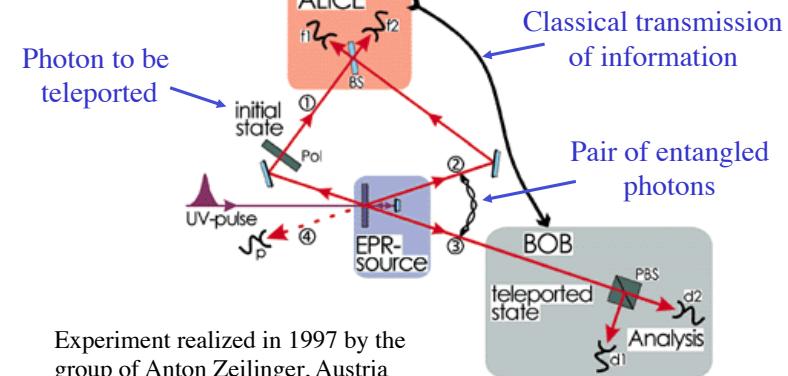
where

$$|\Phi^\pm\rangle_{12} = \frac{1}{\sqrt{2}}(|0\rangle_1|0\rangle_2 \pm |1\rangle_1|1\rangle_2)$$

$$|\Psi^\pm\rangle_{12} = \frac{1}{\sqrt{2}}(|0\rangle_1|1\rangle_2 \pm |1\rangle_1|0\rangle_2)$$

Bennett, Brassard, Crepeau, Josza, Peres, Wooters 1993

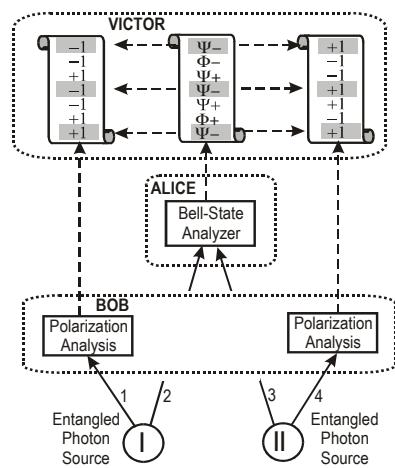
## Quantum Teleportation with Photons



Experiment realized in 1997 by the group of Anton Zeilinger, Austria

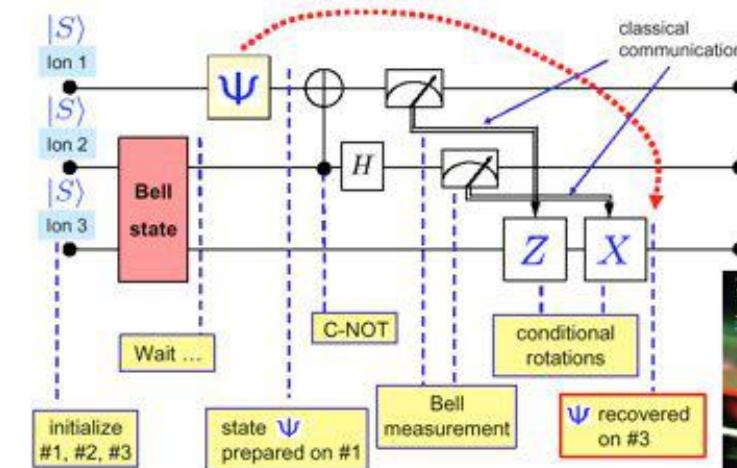
Drawback of this scheme: only one Bell state out of 4 can be identified

## Entanglement swapping

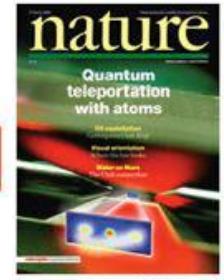


- Two entangled pairs 12 and 34
- Bell measurement by Alice on photons 2 and 3
- Photon 1 and 4 become entangled without having ever met !
- This can be checked using a Bell test between 1 and 4.
- With photons + beam-splitter + counters the Bell state analysis remains incomplete

## Teleportation protocol



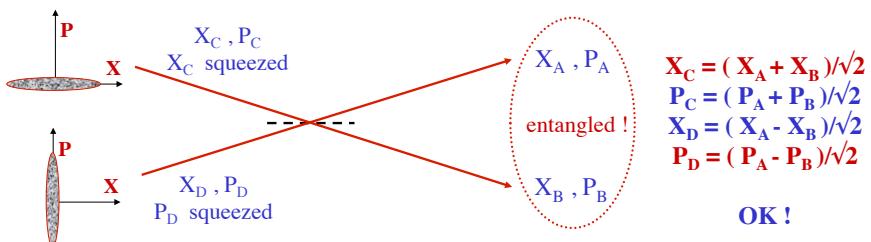
Innsbruck University  
+  
NIST Boulder 2004



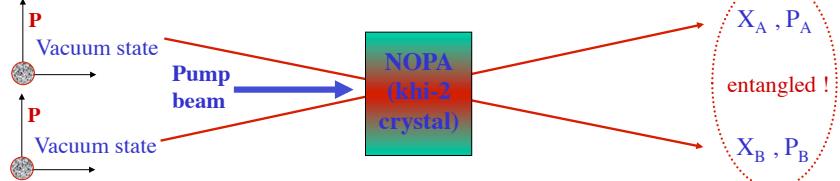
17 June 2004

## How to produce CV entangled beams ?

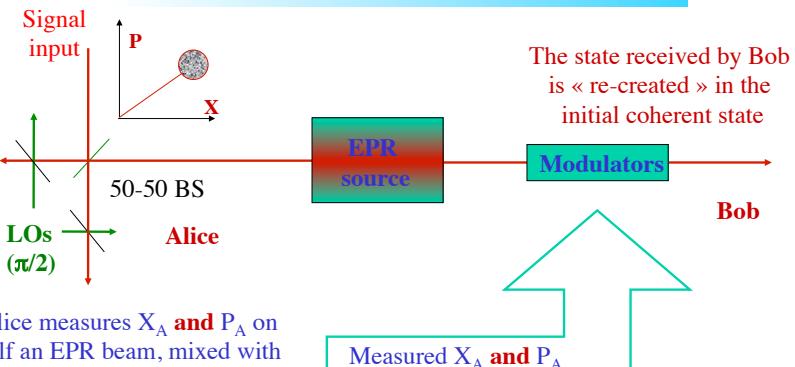
### 1. Combine two orthogonally squeezed beams



### 2. Use a Non-degenerate Optical Parametric Amplifier (NOPA)



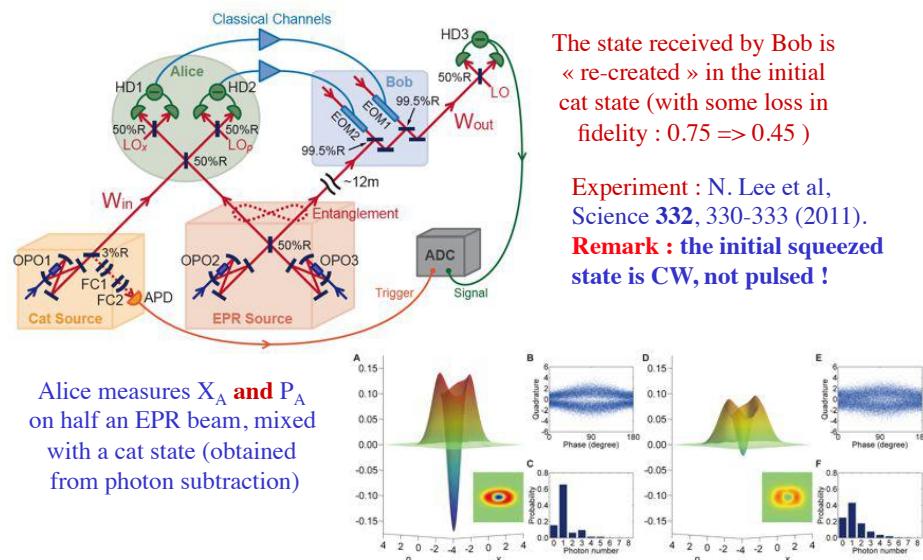
## Quantum teleportation of coherent states



Experiments :

- A. Furusawa et al, Science **282**, 706 (1998)
- W. Bowen et al, Phys. Rev. A **67**, 032302 (2003)
- T.C. Zhang et al, Phys. Rev. A **67**, 033802 (2003)

## Quantum teleportation of cat states



## Advances in Quantum Teleportation

arXiv:1505.07831

Stefano Pirandola, Jens Eisert, Christian Weedbrook, Akira Furusawa, Samuel L. Braunstein

Quantum Technology	Efficiency	Fidelity	Distance	Memory
Photonic qubits	$\leq 50\%$ <sup>†</sup>	$\gtrsim 83\%$ <sup>22</sup>	143 km <sup>22</sup>	N/A <sup>‡</sup>
	25%	81% <sup>23</sup>	6 km fibre <sup>24</sup>	
	1/27	89% <sup>25</sup>	On chip	
	1/32	$\gtrsim 57\%$ <sup>26</sup>	Table-top	
NMR <sup>28</sup>	100%	$\approx 90\%$ <sup>27</sup>	$\approx 1\text{ \AA}$	$\approx 1\text{ s}$
Optical modes	CVs <sup>29-36</sup>	83% <sup>36</sup>	12 m <sup>35</sup>	N/A <sup>‡</sup>
	Hybrid <sup>37</sup>	$\gtrsim 80\%$	Table-top	
Atomic ensembles	(hot) CV light-to-matter <sup>38</sup>	58%	Table-top	4 ms <sup>33</sup>
	(hot) CV matter-to-matter <sup>39</sup>	$\gtrsim 55\%$	0.5 m	
	(cold) DV light-to-matter <sup>40</sup>	78%	7 m fibre	
	(cold) DV matter-to-matter <sup>41</sup>	88%	150 m fibre	
Trapped atoms	Trapped ions <sup>42-44</sup>	83% <sup>44</sup>	5 $\mu\text{m}$ <sup>43</sup>	$\simeq 50\text{ s} \star^{33}$
	Trapped ions & photonic carriers <sup>45</sup>	90%	1 m	
	Neutral atoms in an optical cavity <sup>46</sup>	88%	21 m fibre	
Solid state	Frequency qubit to quantum dot <sup>47</sup>	25%	78% <sup>5</sup>	$\gtrsim 1\text{ }\mu\text{s} \star^{137}$
	Polarisation qubit to rare-earth crystal <sup>48</sup>	25%	89%	
	Superconducting qubits on chip <sup>49</sup>	77%, 69% <sup>49</sup>	10 m, 24.8 km fibre <sup>50</sup>	
	Nitrogen-vacancy centres in diamonds <sup>50</sup>	100%	On chip (6 mm)	
			$\lesssim 100\text{ }\mu\text{s} \star^{139,140}$	$\lesssim 0.6\text{ s} \star^{141}, \gtrsim 1\text{ s} \star^{134}$

### Part 1 - Quantum optics with discrete and continuous variables

- 1.1 Homodyne detection and quantum tomography
- 1.2 Generating non-Gaussian Wigner functions : kittens, cats and beyond

### Part 2 - Towards optical quantum networks

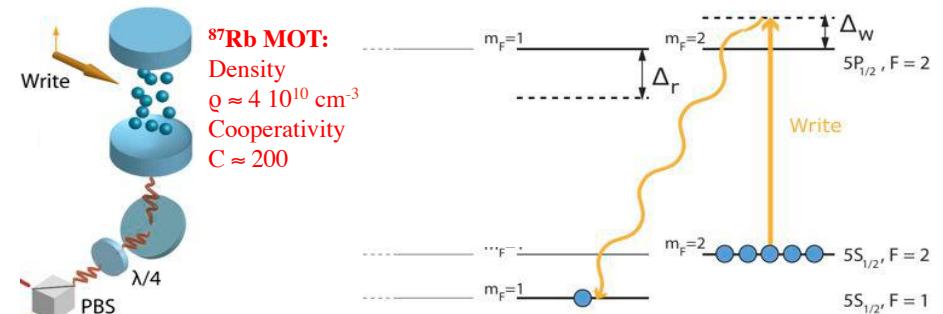
- 2.1 Entanglement, teleportation, and quantum repeaters
- 2.2 Some experimental achievements

### Part 3 - A close look to a nice single photon

- 3.1 Single photons: from old times to recent ones
- 3.2 Experimental perspectives

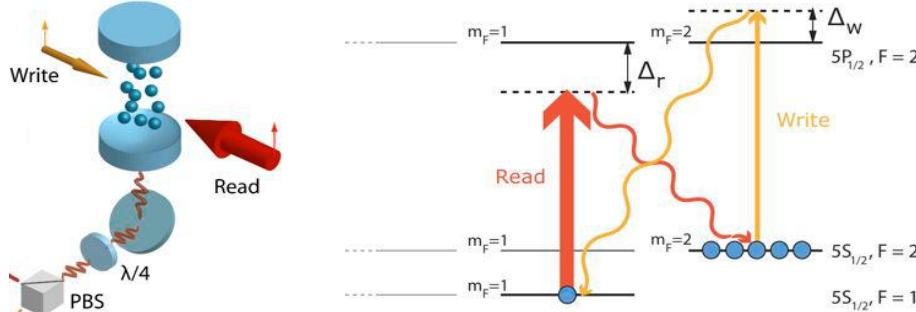
## Single Photon from a single polariton (DLCZ protocol)

L.M. Duan, M.D. Lukin,  
J.I. Cirac, and P. Zoller,  
Nature 414, 413 (2001)



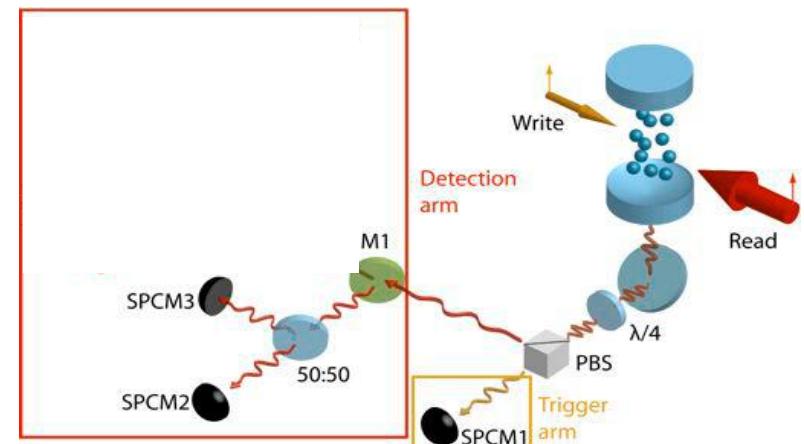
E. Bimbard et al, arXiv:1310.1228 (2013), PRL 112, 033601 (2014)

## Single Photon from a single polariton (DLCZ protocol)

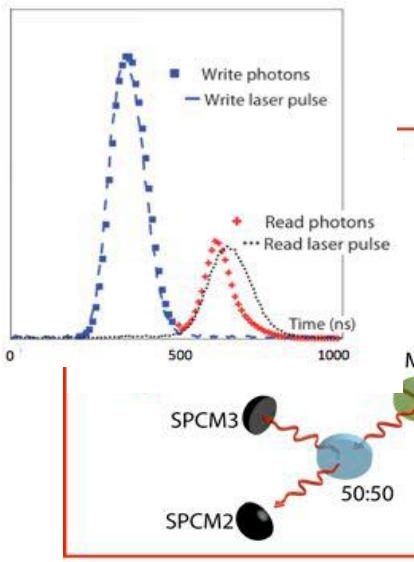


E. Bimbard et al, arXiv:1310.1228 (2013), PRL 112, 033601 (2014)

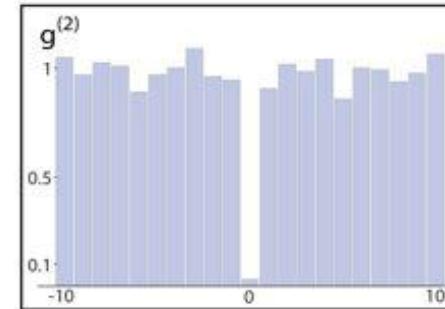
## Single Photon from a single polariton (DLCZ protocol)



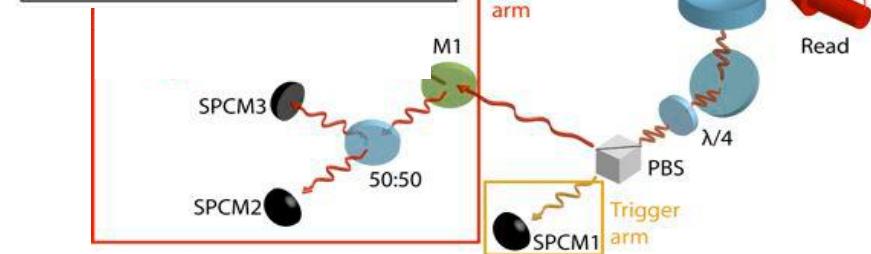
E. Bimbard et al, arXiv:1310.1228 (2013), PRL 112, 033601 (2014)



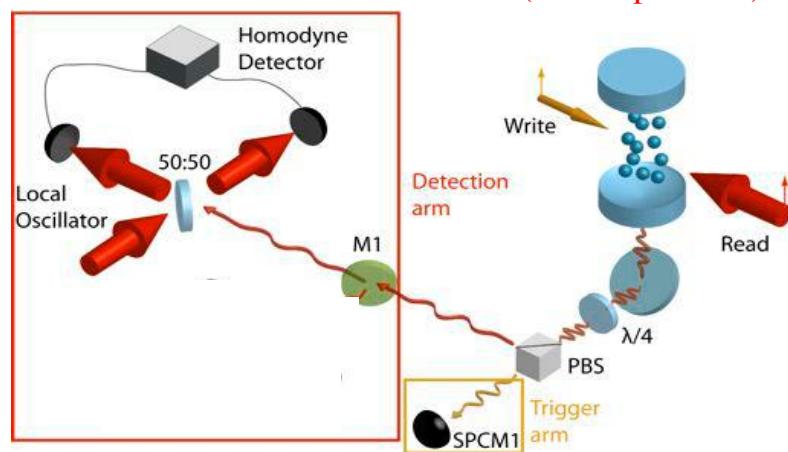
Single Photon from a single polariton (DLCZ protocol)



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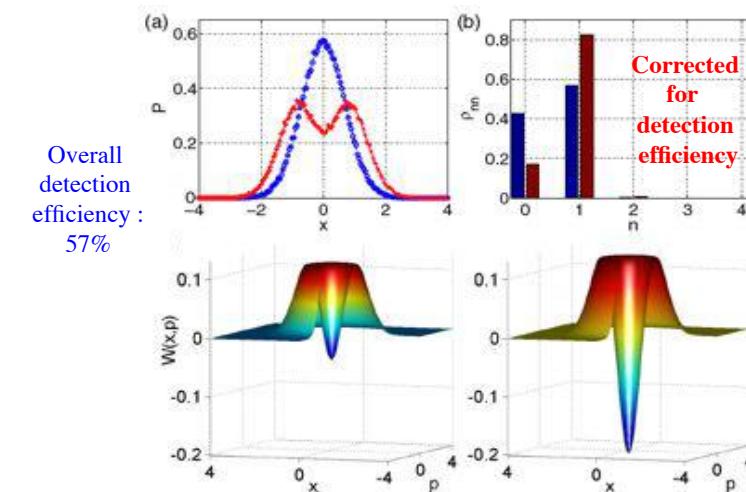


E. Bimbard et al, arXiv:1310.1228 (2013), PRL 112, 033601 (2014)



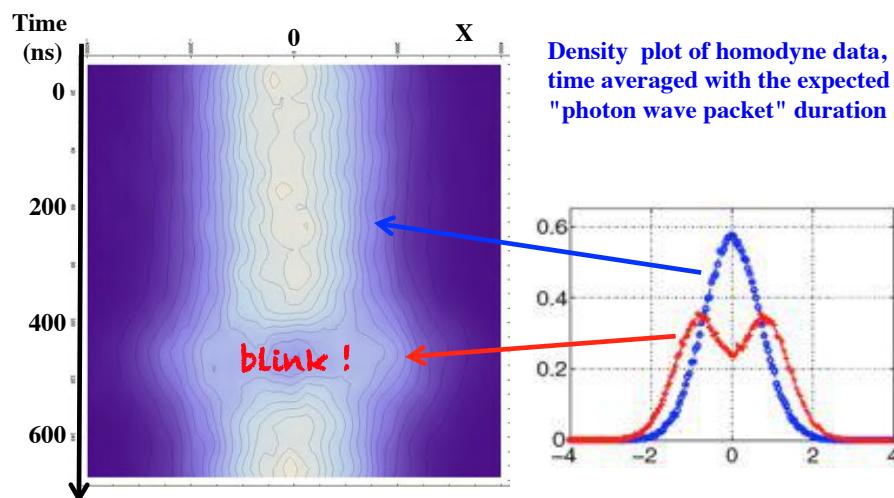
Single Photon from a single polariton (DLCZ protocol)

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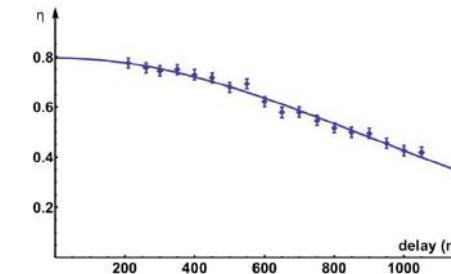
E. Bimbard et al, arXiv:1310.1228 (2013), PRL 112, 033601 (2014)

## Looking at the Blinking Photon



## Single Photon from a single polariton (DLCZ protocol)

Quantum memory effect : the memory time ( $1 \mu\text{s}$ ) is limited by motional decoherence due to finite temperature ( $50 \mu\text{K}$ )



$$\eta = P_{\text{Doppler}}(t) \times P_{\text{Coop}} \times P_{\text{Read}} \times P_{\text{Pumping}} \times P_{\text{Mode}} \times P_{\text{Cav}}$$

$$0.94 \times 0.97 \times 0.96 \times 0.965 \times 0.97 = \underline{\underline{0.82 : \text{ok!}}}$$

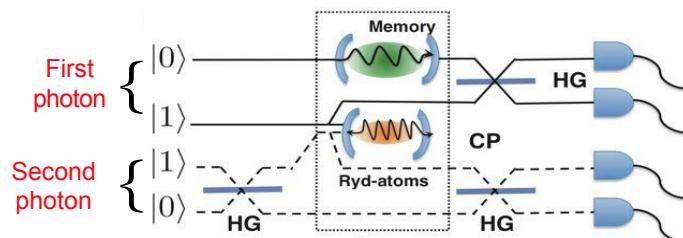
E. Bimbard et al, arXiv:1310.1228 (2013), PRL 112, 033601 (2014)

## Photonic Controlled-Phase Gates Through Rydberg Blockade in Optical Cavities

S. Das, A. Grankin, I. Iakoupor, E. Brion,  
J. Borregaard, R. Boddeda, I. Usmani, A. Ourjoutsev,  
P. Grangier, A. S. Sørensen, arxiv:1506.04300



Dual-rail photonic gate (used here for a Bell measurement)



Significant increase in the swap efficiency in a quantum repeater scheme, compared to linear quantum gates (with efficiency bounded to 50%)  
**=> secret bit rate increased by about one order of magnitude.**

See also : J. Borregaard et al, arXiv:1504.03703 (2015).



## (Temporary) Conclusion

### Many potential uses for Quantum Continuous Variables...

- \* Conditional preparation of « squeezed » non-gaussian pulses / cats
- \* Big family of phase-dependant states with negative Wigner functions !
- \* Many new experimental results...
- \* Quantum cryptography
- \* Coherent states protocols using reverse reconciliation, secure against any (gaussian or non-gaussian) collective attack
- \* Working fine in optical fibers @1550 nm (SECOQC, SeQureNet...)
- \* Quantum repeaters
- \* Basic elements do work in proof-of-principle experiments...
- \* ... but not well enough yet to get a whole system with acceptable efficiency.
- \* So more work is needed, both on theory and implementations...